

## **\*MECHANICS OF POLYMER SOLIDS AND FLUIDS**

**ChBE/MSE/ME 7771**

Tuesdays, Thursdays: 5:00 pm – 6:15 pm  
Ford Environmental Sci & Tech L1175

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Please use Canvas for all email communications.

### **Learning/Teaching Objectives:**

- (1) Provide students in Polymer Science & Engineering, Chemical Engineering and Materials Science and Engineering and Mechanical Engineering with a basic knowledge of the behavior of polymeric solids
- (2) Enable students to use fundamental principles to solve real manufacturing problems related to plastic flow
- (3) Provide students in Polymer Science and Engineering, Chemical Engineering, Materials Science and Engineering and Mechanical Engineering with a thorough and comprehensive background of polymeric flow as non-Newtonian fluid mechanics and rheology.
- (4) Enable students to use fundamental principles to solve real manufacturing problems and rheology for polymers
- (5) Introduce computational techniques to simulate problems in rheology

**Prerequisites:** Basic courses on mechanics of solids and fluids; exposure to differential equations, tensor algebra and calculus, and computer programming are helpful, although not required.

### **Reference Books:**

Theory of Elasticity, Sokolnikoff  
Theory of Elasticity, Timoshenko  
Mechanical Properties of Solid Polymers, I. M. Ward  
The Mathematical Theory of Plasticity, Hill  
Plasticity, Theory and Application, Mendelson  
Foundations of Solid Mechanics, Y.C. Fung  
Advanced Fracture Mechanics, M. F. Kanninen and C. H. Poplar  
The Structure and Rheology of Complex Fluids, R. G. Larson  
Introduction of Fluid Dynamics, S. Middleman  
Transport Phenomena, R. B. Bird, W. E. Stewart, E. N. Lightfoot  
Principles of Non-Newtonian Fluid Mechanics, G. Astarita, G. Marrucci  
**An Introduction to the Mechanical Properties of Solid Polymers 2nd Edition, I. M. Ward (Author), J. Sweeney, Wiley**

**Dynamics of Polymeric Liquids, Vol I, 2 nd edition, R. B. Bird, R. C. Armstrong, O. Hassager, Wiley-Interscience**

Handouts from various solid mechanics books will be given. The last two books are ones directly related to this course, especially the last one. It is a very good book, but somewhat expensive. But there are cheaper options such as renting.

Two main sections:

Foundations of Mechanics, constitutive equations of solids (~30%), various fluids, and their flow characteristics, otherwise called Rheology (~70%)

**(1) Basic Framework for Solid Mechanics**

Indicial notation, force balance & momentum balance, state of stress, principal stresses

**(2) Constitutive Equations for Solids (stress-strain behavior of polymers)**

Material symmetry & anisotropy, large deformation & non-linearity

**(3) Failure Conditions for Polymers, Yield and Post Yield Behavior (Flow of Solids)**

Yielding, three-dimensional yield conditions, especially Tresca and von Mises yield criterion

Plasticity, flow rule, loading & unloading behavior, consistency condition

Strain hardening

Mullins and Payne effects in polymer systems

Dynamics of polymer solution and melt (non-Newtonian fluids – 70 to 80%)

**(1) Framework of Fluid Mechanics**

Mass and momentum balance equations; energy equations; kinematics; and boundary conditions.

**(2) Non-Newtonian Fluids (Rheology)**

Structure of Polymeric Fluids

Flow Phenomena in Polymeric Fluids

Material Functions

Steady Shear Flow

Small Amplitude Oscillatory Flow

Inception of Steady Shear Flow

Cessation of Steady Shear Flow  
Sudden Shearing Displacement  
Creep  
Constrained recoil  
Constitutive Equations

**(3) Generalized Newtonian Fluids**

Concept of Generalized Newtonian Fluids  
Viscometric Flow  
Power law, Ellis, Carreau-Yashuda, Bingham plastic fluids, etc.

**(4) Numerical Methods**

Calculus of Variations  
Weighted Residual Method  
Finite Element Method  
Applications using commercial software  
Development of computer programs (just introduction due to lack of time)

**(5) General Linear Viscoelastic Fluids**

Generalized Maxwell Fluid  
Jeffrey's Model  
Differential and Integral Representations  
Turn Table Experiment

**(6) Convected and Corotational Models for Polymeric Fluids**

Convected Derivatives  
    Upper Convected Models  
    Lower Convected Models  
    Jaumann Co-rotational Models  
Ordered Fluids  
Criminale-Ericksen-Filbey Fluids  
Reiner-Rivlin Fluids, etc

**(7) Quasi-Linear Differential Models for Polymeric Fluids**

Convected Maxwell Model  
Oldroyd's Fluid A and B  
White-Metzner Fluid  
Oldroyd 8-Constant Model  
Giesekus Fluid  
Johnson-Segalman Fluids, etc.

**(8) Integral Forms**

Single Integral Constitutive Equations  
Quasi-Linear Integral Models  
Non-Linear Integral Constitutive Equations  
    K-BKZ Equation  
    Rivlin-Sawers Equation  
    Doi-Edwards Equation  
Memory Integral Expansions

**(9) Introduction to the Kinetics of Polymeric Liquids**

Dumbbell, bead-spring chain, bead-rod-spring models

**(10) Anisotropic Polymeric Fluid Flow (\*Time permitting)**

Introduction to liquid crystals, anisotropic (LC) flow, pattern formation, Ericksen-Leslie theory, molecular theory of Leslie viscosities, introduction to nematic and smectic crystal flow.

**(11) Numerical Applications (\*Time permitting)**

Solution to Boundary Value/Initial Value Problems  
Development of Computer Algorithms  
Simulation using POLYFLOW, FIDAP, etc.  
    Fiber Spinning  
    Mold Filling, etc.

**(12) Current Developments (\*As time permits)**

**Grading Policy:**

Two in-class tests.

Finals: In-class comprehensive, but only 1 and ½ hours long.

One 4x6 inch index card is allowed during the tests, writing both sides is allowed

Composite score calculation: 5 % Homework, 30 % for each quiz, 30 % Finals

There will be five random very short quiz (probably taking five minutes or less)

each with one point (total 5 points). For the quiz, only a genuine effort will be graded, no requirement for correct answers.

HW is graded primarily for demonstrating the thought process and effort, not necessarily for correct answers.

	<i>Scores between Letter grade</i>	
Grading Policy:	90 – 100	A
	80 – 89	B
	70 – 79	C
	60 – 69	D etc.

However, if the class average is below 80, scores will be scaled to bring the class average to 80 and the highest score to 100. If the class average is above 80, scores won't be curved, unless the highest score is well below 100 (below 90 for example).

**Important dates: (based on information we have now)**

<https://registrar.gatech.edu/future-academic-calendar>

Fall Break: Oct 5,6

Withdrawal Deadline: Oct 31

Final Exam: TBD

[https://registrar.gatech.edu/public/files/Final%20Exam%20Matrix%20for%20Fall%202025\\_2.pdf](https://registrar.gatech.edu/public/files/Final%20Exam%20Matrix%20for%20Fall%202025_2.pdf) (for 2025)

Tentative dates of tests: September 24 and October 29, to be confirmed.

If anyone had to miss one test for an approved excuse, the score for that test will be replaced by the scaled (based on the class average) scores from other tests.

Any changes in syllabus, if required, will be announced with adequate notice.

**Required Items (From Georgia Tech Policy)**

Students with special needs and accommodations, please contact the Office of Disability Services <https://disabilityservices.gatech.edu/>

Acceptable conduct: Student Faculty Expectations <https://catalog.gatech.edu/rules/22/>

Academic integrity: Follow Georgia Tech Honor Code <https://policylibrary.gatech.edu/student-life/academic-honor-code>